

# Parameter identification of a tumor model using artificial neural networks

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## 2 Theoretical background and motivation

- Problem
- Neural Network
- Tumor model

## 3 Results of parameter estimation

- The neural networks used for parameter estimation
- Neural network estimating pharmacokinetic parameters
- Neural network estimating tumor dynamics parameters

## 4 Conclusions

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## 4 Conclusions

# Therapy optimization



## Medical knowledge



cancer treatments

general protocols



## Healing of the patient

find more effective solutions in healing

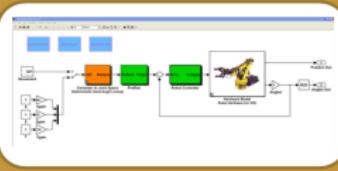
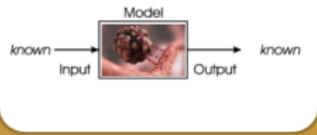
individual treatment for the patient

model identification

model-based protocols



## Engineering knowledge



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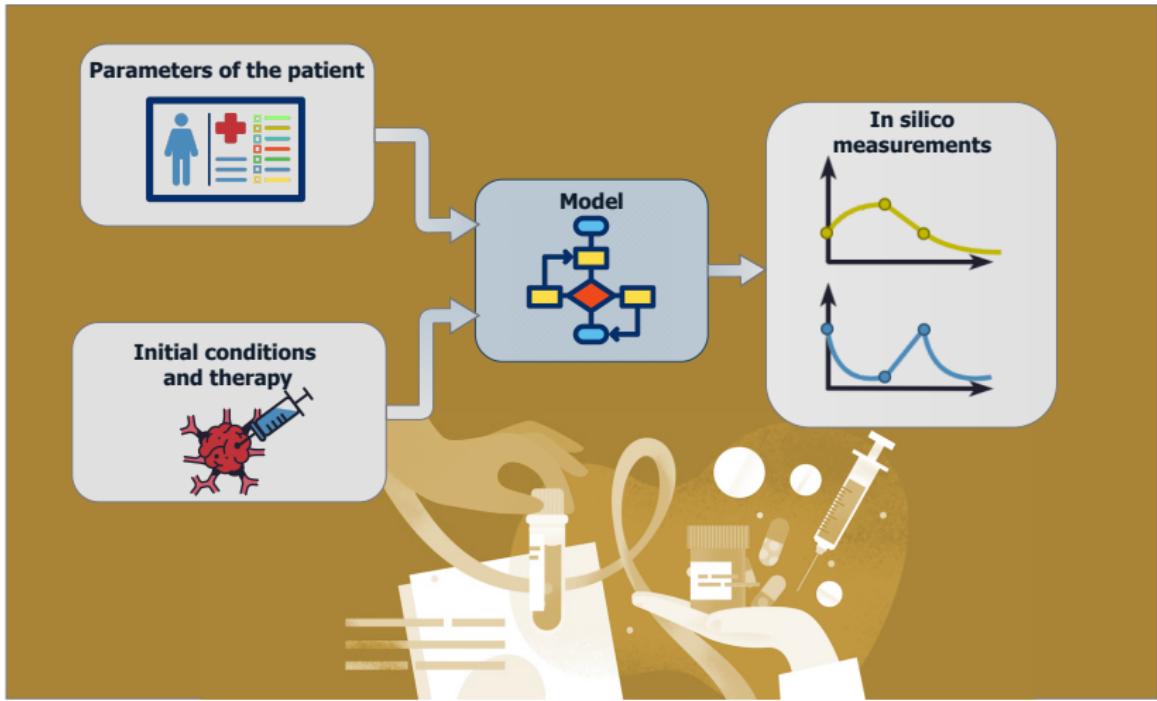
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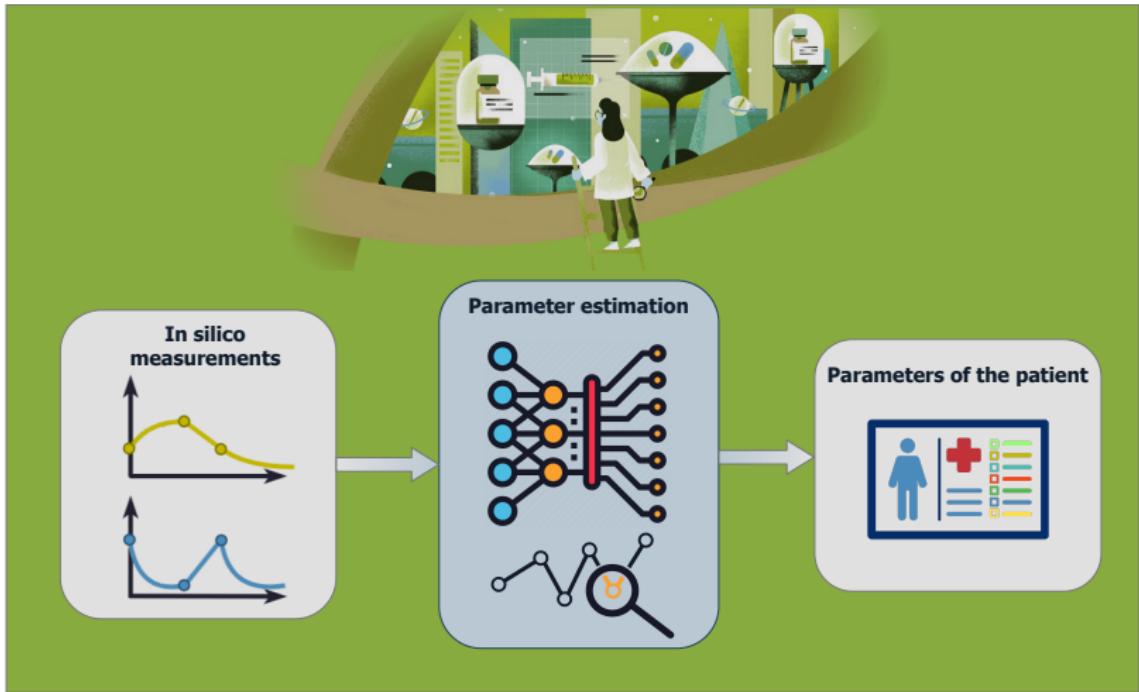
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# In silico measurement generation



# Goal: parameter estimation



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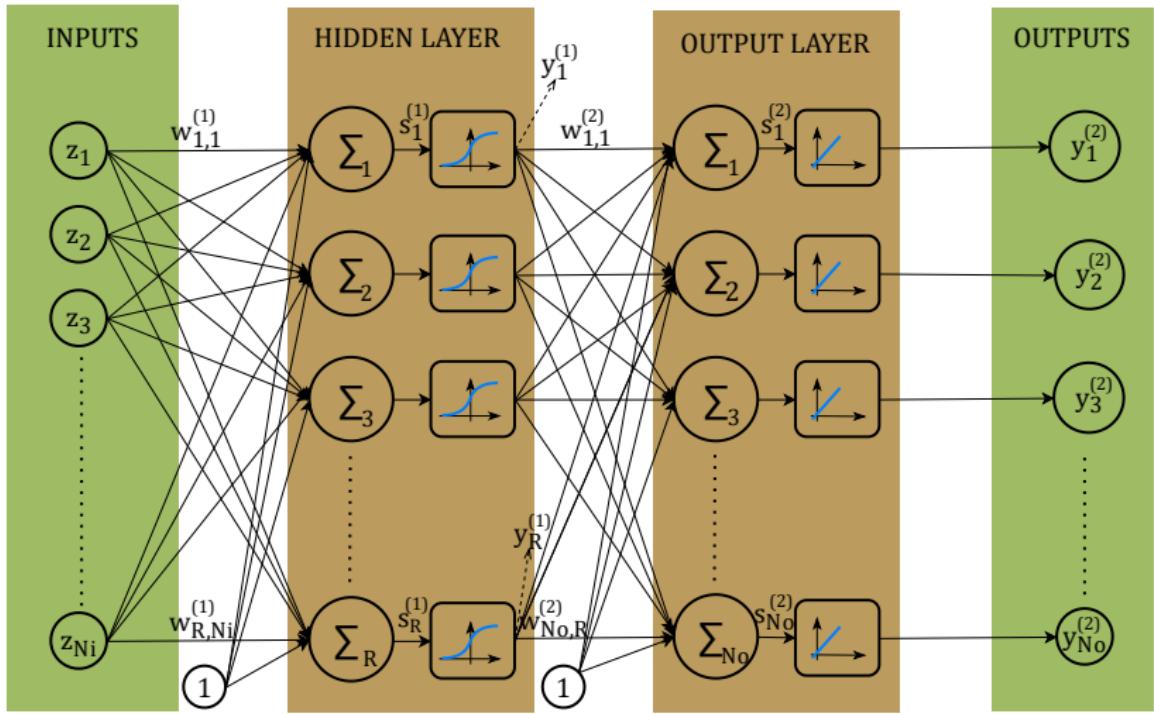
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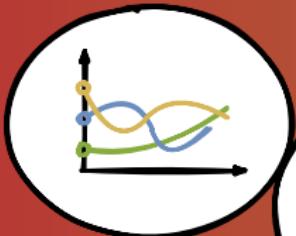
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# Feedforward, two-layer architecture



# Applications

I.



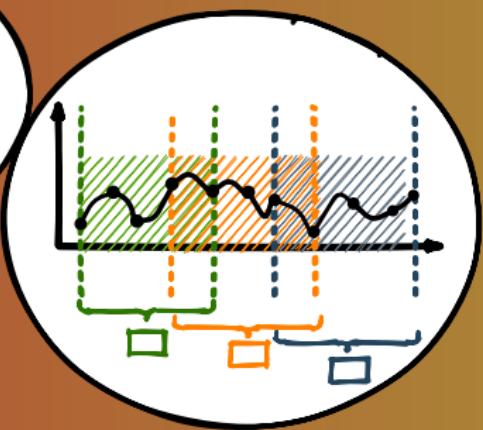
Parameter  
estimation

II.



Experiment  
design

III.



Moving horizon estimation

# Applications

## Applications of neural networks and their training

- Initial estimation for local identification algorithms.
- Numerical identification analysis based on training results → used for experiment design.
- Moving horizon estimation to follow parametric changes.

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# Physiological processes as fictive chemical reactions

## Reaction steps and the modeled physiological phenomena

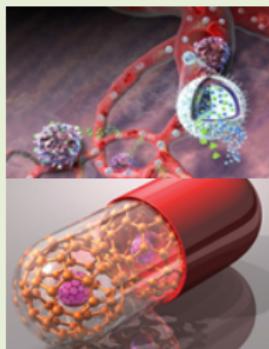
$X_1 \xrightarrow{a} 2X_1$  Tumor cell proliferation

$X_1 \xrightarrow{n} X_2$  Tumor necrosis

$X_1 + X_3 \xrightarrow{b} X_2$  Drug effect

$X_3 \xrightarrow{c} 0$  Drug clearance

$X_3 \xrightleftharpoons[k_2]{k_1} X_4$  Two-compartment model



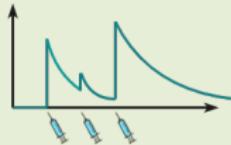
# Differential equations derived from the chemical reaction steps

Differential equations describing tumor dynamics and drug pharmacokinetics and pharmacodynamics, An impulsive system

$$\begin{aligned}\dot{x}_1 &= (a - n)x_1 - b \frac{x_1 x_3}{ED_{50} + x_3} \\ \dot{x}_2 &= nx_1 + b \frac{x_1 x_3}{ED_{50} + x_3} - wx_2 \\ \dot{x}_3 &= -(c + k_1)x_3 + k_2 x_4 - b_\kappa \frac{x_1 x_3}{ED_{50} + x_3} + u \\ \dot{x}_4 &= k_1 x_3 - k_2 x_4\end{aligned}$$



$$y = x_1 + x_2 \iff x_3(t_k^+) = x_3(t_k^-) + \kappa d_k \implies$$





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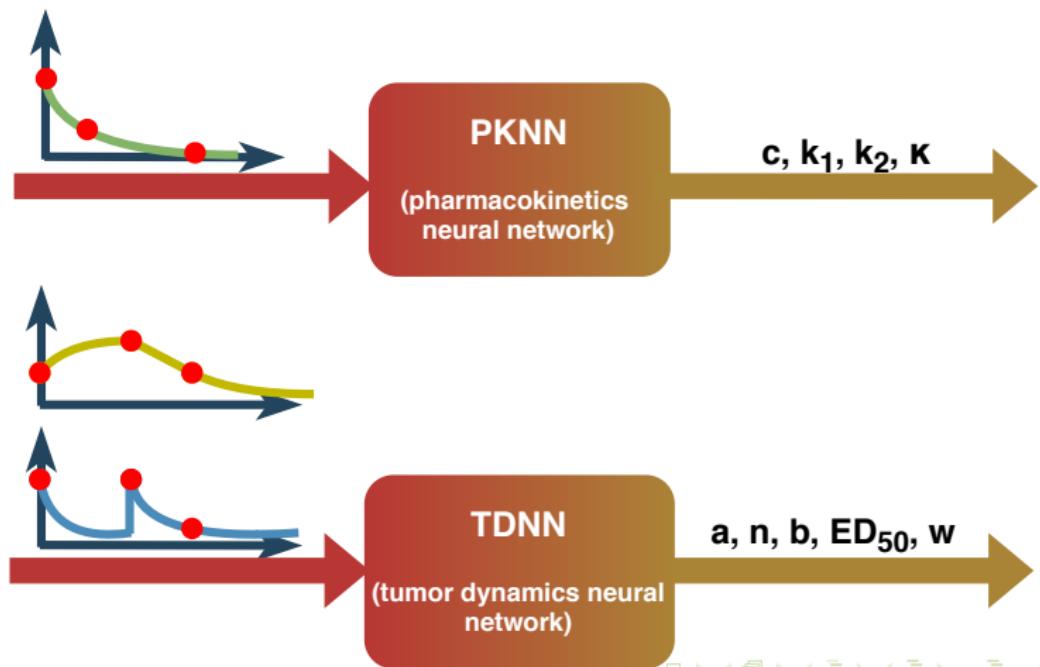
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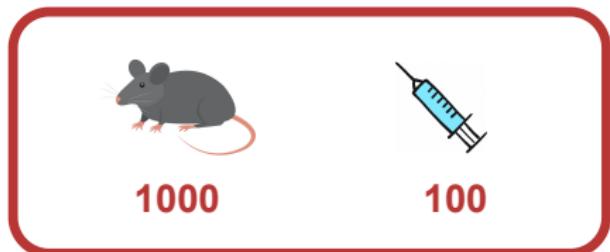
# Two neural network type, for different measurements and parameters



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# Training data for PhamacoKinetics Neural Network (PKNN)



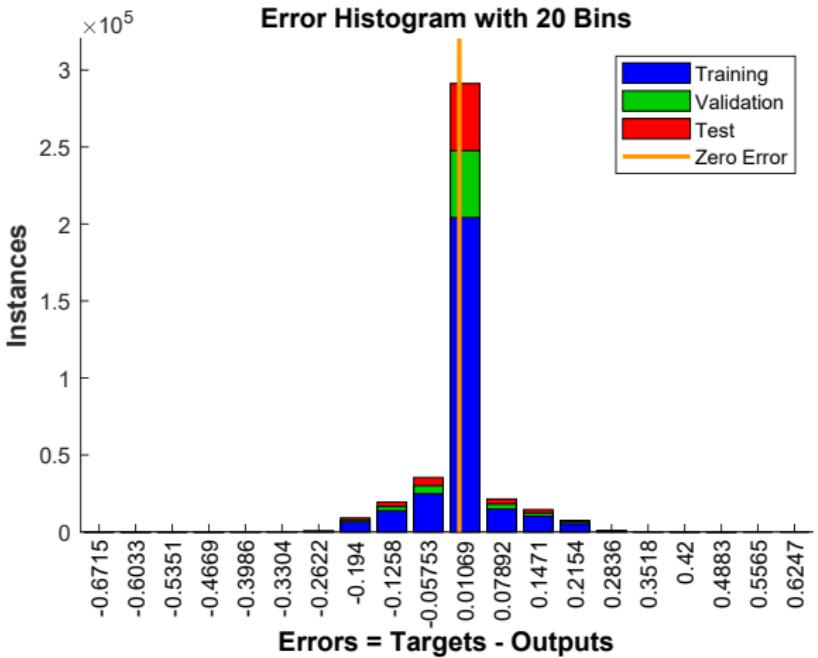
Training data	Validation data	Test data
70%	15%	15%

Sampling: 5 minutes after injection, then every 9 minutes

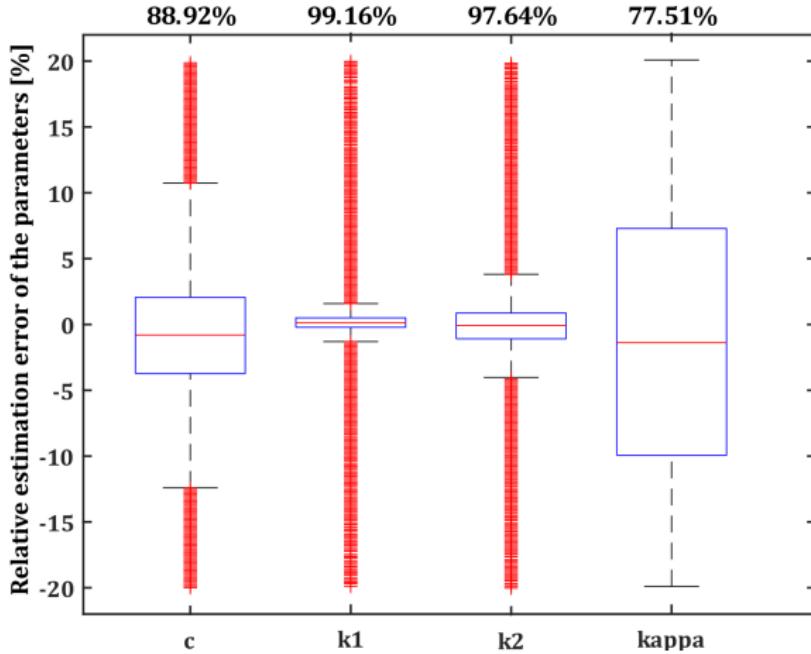
Number of measurements



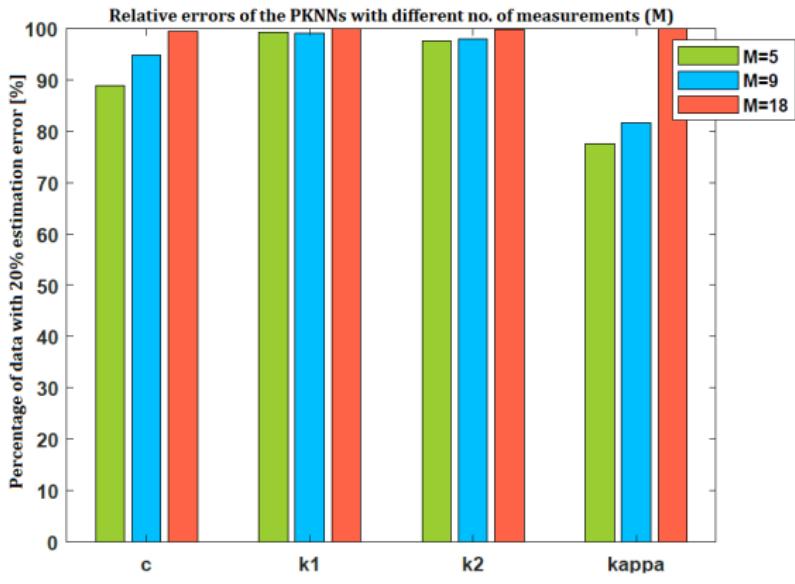
# PKNN error histogram estimation from five measurements



# The estimation errors between $\pm 20\%$ error interval for the PKNN



# Comparison of PKNN networks estimating from different number of measurements performing on $\pm 20\%$ error interval



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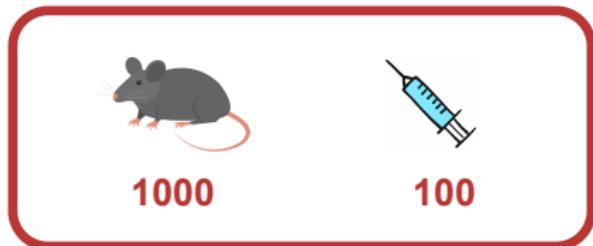
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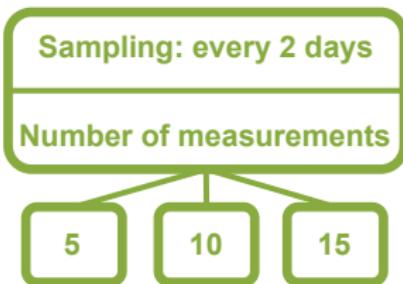
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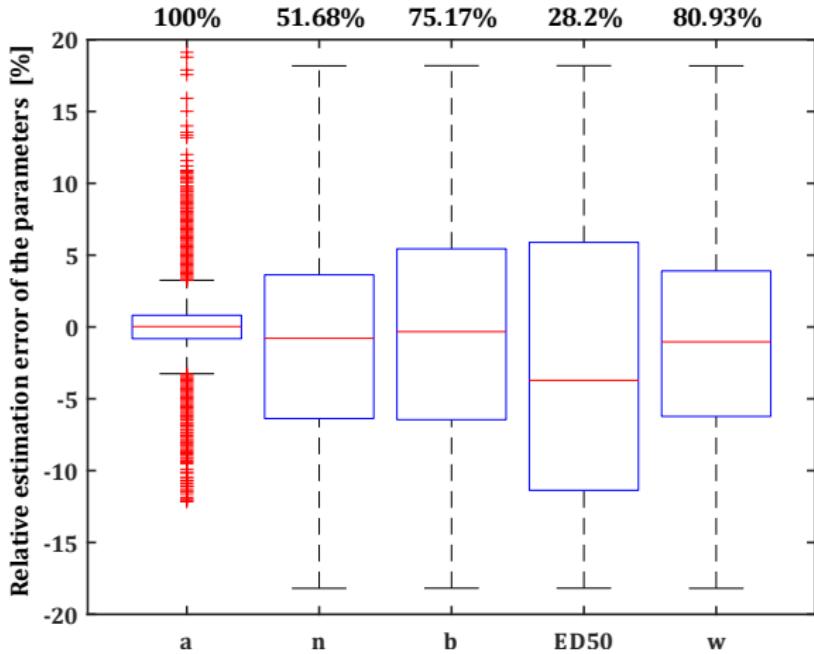
# Training data for Tumor Dynamics Neural Network (TDNN)



<b>Training data</b> 70%	<b>Validation data</b> 15%	<b>Test data</b> 15%
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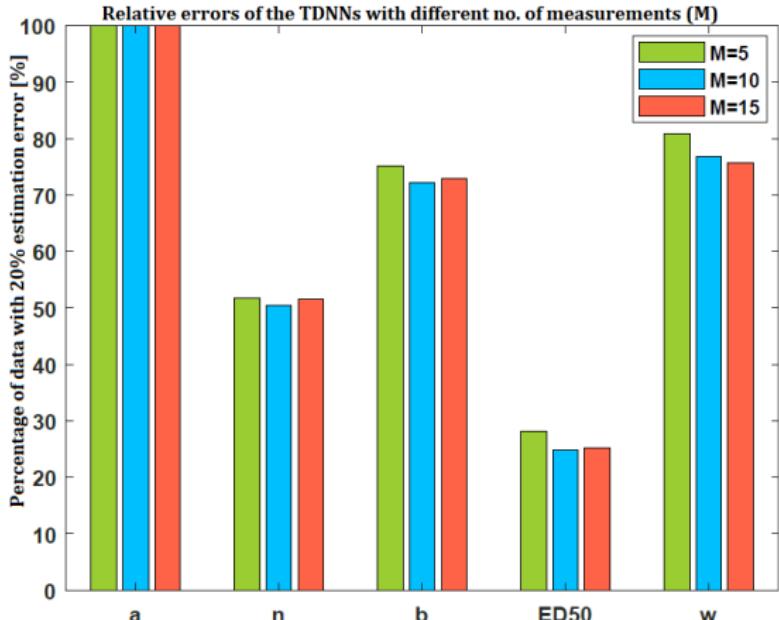


# The estimation errors between $\pm 20\%$ error interval for the TDNN





Comparison of TDNN networks estimating from different number of measurements performing on  $\pm 20\%$  error interval



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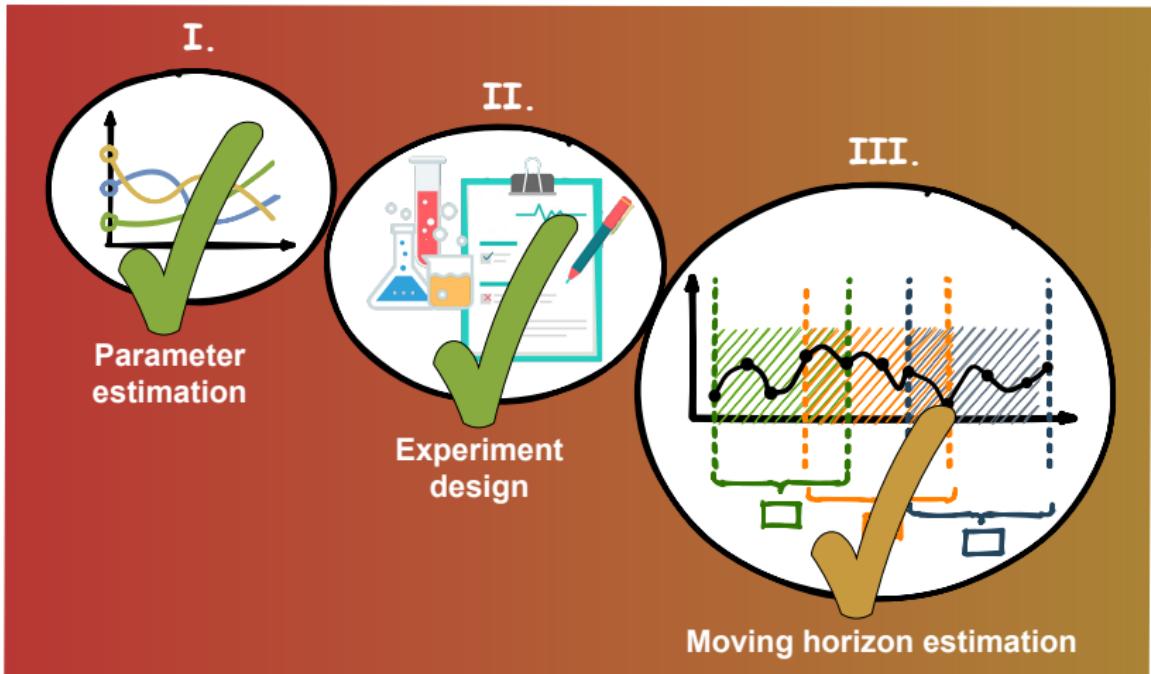
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## Main results

- Most parameters can be estimated with good accuracy → can be used as initial conditions by local algorithms
- Some parameters can not be estimated properly → different experimental setups are required.
- Small number of measurements is enough for estimation → moving horizon estimation is possible (future works).

# Thank you for your attention!

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